Energetic Approach to the Folding of α/β Barrels

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ABSTRACT The folding of a polypeptide into a parallel $(\alpha/\beta)_8$ barrel (which is also called a circularly permuted $\beta_8\alpha_8$ barrel) has been investigated in terms of energy minimization. According to the arrangement of hydrogen bonds between two neighboring β-strands of the central barrel therein, such an α/β barrel structure can be folded into six different types: (1) left-tilted, left-handed crossover; (2) left-tilted, right-handed crossover; (3) nontilted, left-handed crossover; (4) nontilted, right-handed crossover; (5) right-tilted, left-handed crossover; and (6) right-tilted, right-handed crossover. Here "tilt" refers to the orientational relation of the β-strands to the axis of the central β-barrel, and "crossover" to the βαβ folding connection feature of the parallel β-barrel. It has been found that the right-tilted, right-handed crossover α/β barrel possesses much lower energy than the other five types of α/β barrels, elucidating why the observed α/β barrels in proteins always assume the form of right tilt and right-handed crossover connection. As observed, the β-strands in the energy-minimized right-tilted, right-handed crossover $(\alpha/\beta)_8$-barrel are of strong right-handed twist. The value of root-mean-square fits also indicates that the central barrel contained in the lowest energy $(\alpha/\beta)_8$ structure thus found coincides very well with the observed 8-stranded parallel β-barrel in triose phosphate isomerase (TIM). Furthermore, an energetic analysis has been made demonstrating why the right-tilt, right-handed crossover barrel is the most stable structure. Our calculations and analysis support the principle that it is possible to account for the main features of frequently occurring folding patterns in proteins by means of conformational energy calculations even for very complicated structures such as $(\alpha/\beta)_8$ barrels.

Key words: staggering hydrogen bonds, tilt, twist, βαβ crossover connection, random generation of initial structures, energy minimization, associated loop energy

INTRODUCTION

From the aesthetical point of view, the α/β barrel structure is probably one of the most striking struc-

tures in proteins. Such a beautiful structure is constructed as if by successively folding a chain, alternating between β-strands and α-helices, into a cylindrical topology suggesting the general shape of a barrel. Triose phosphate isomerase (TIM) was the first example of a protein found to have this type of structure.[1,2] So far these structures are known to occur in 17 enzymes,[3] all with little sequence homology, but significant structural similarity,[3,4] i.e., all with 8 parallel β-strands as an "inner core" surrounded by 7 or 8 α-helices as an "outer concentric cylinder." Each inner β-strand is connected to an outer α-helix in a right-handed βαβ crossover manner,[5,6] so to a first approximation the enzyme can be expressed as an $(\alpha/\beta)_8$ structure.[3] Although this structure motif is termed a barrel, the cross section of the barrel is usually elliptical rather than circular.[3] Rather than being parallel to the central axis of the β-barrel, both the inner β-strands and the outer α-helices are tilted so as to follow a right-handed spiral around the central axis of the barrel,[7–10] as reflected by having a positive shear number introduced by McLachlan.[9] An α/β barrel structure with such features in tilt and crossover connection is called the *right-tilted, right-handed crossover α/β-barrel*, as will be further described later. The topology of α/β barrels is almost invariant, with each connection moving over by one strand and always in the same direction (right-handed as referred to the strand direction), which is why they are called singly wound barrels.[11] As pointed out recently by Farber and Petsko,[3] of the enzymes whose structure is known, roughly 1 of 10 has this kind of α/β domain, indicating the importance of understanding this type of structure.

The existence of such a set of similar structures, arising from proteins with very dissimilar sequences, poses such a questions: why are the folds so similar? Lasters et al.[12,13] used a geometric model and the requirements of close packing to demonstrate that the 8-fold parallel barrel was one of only

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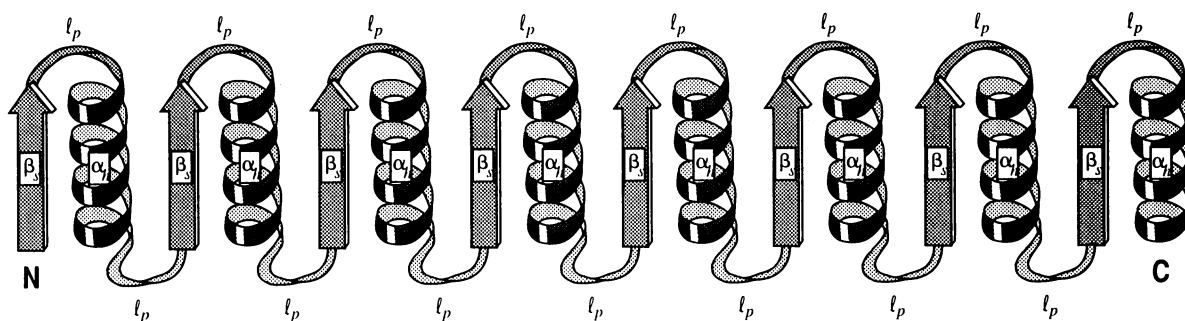
Fig. 1. Schematic illustration of a polypeptide chain in which β_s represents a β-strand and α_h represents α-helices. Between the adjacent β_s and α_h segments along the chain there is a link ℓ_p, which will become a loop after the polypeptide chain is folded into an α/β barrel. The number of β_s segments and the number of α_h segments are the same, both equal to $n_b = 8$, and the number of ℓ_p segments is $(2n_b - 1) = 15$.

a few viable barrel conformations. Lesk et al.[2] analyzed the packing of the residues in the interior of α/β barrels, and found that not all proteins with this fold are related by evolution, but that they represent a common favorable solution to the structural problems involved in the creation of a closed β-barrel. Recently, de novo design of an α/β barrel protein has also been engineered by Luger et al.[14] and Goraj et al.[15] in order to address this issue. On the other hand, based on structural and chemical evidence, it was proposed by Farber and Petsko[3] that all of these α/β barrel domains may have diverged from a common ancestor. To the best of our knowledge, however, so far no quantitative analysis has been reported on the energetic features of such a folding motif.

The present study was initiated in an attempt to quantitatively address the issue from an energetic point of view. Our discussions were focused on the following points: What is the major factor that stabilizes the right-tilted, right-handed crossover α/β barrel? What role do the α-helix segments play? What role do the β-strand segments play? What role do the loop segments, which sequentially connect the α-helices and β-strands along the chain folded into the α/β structure, play? What role do the interactions among these three components play? Can an α/β barrel with other handed features be folded as a stable structure?

CLASSIFICATION OF α/β BARRELS

Let us consider a polypeptide chain (Fig. 1) in which there are n_b β-strands (β_s) and n_b α-helices (α_h). Between the adjacent β-strand and α-helix along the chain there is a link (ℓ_p), which will become a loop after the polypeptide chain is folded into an α/β barrel. The number of ℓ_p segments in the polypeptide chain is $2n_b - 1$.

According to the tiltedness of the central β-barrel[16,17] and the chirality of the $\beta\alpha\beta$ crossover connection,[5,6] such a polypeptide chain can be folded

into the following six different types of α/β barrel structures:

1. Left-tilted, left-handed crossover α/β barrel, as symbolized by B_{ll}.
2. Left-tilted, right-handed crossover α/β barrel, as symbolized by B_{lr}.
3. Nontilted, left-handed crossover α/β barrel, as symbolized by B_{nl}.
4. Nontilted, right-handed crossover α/β barrel, as symbolized by B_{nr}.
5. Right-tilted, left-handed crossover α/β barrel, as symbolized by B_{rl}.
6. Right-tilted, right-handed crossover α/β barrel, as symbolized by B_{rr}.

In order to find out from an energetic point of view why all the observed α/β barrels in proteins are of right tilt and right-handed crossover connection, it is necessary, as a first step, to establish a technique by which any of the six types of α/β barrels can be generated as desired.

GENERATION OF α/β BARRELS

Because so far all the α/β barrels observed in proteins, except muconate lactonizing enzyme and mandelate racemase in which the last helix is missed, are formed by 8 strands and 8 helices as symbolized by an $(\alpha/\beta)_8$ barrel, let us assign $n_b = 8$. Only L-type amino acids, the natural amino acids, were used in the current study. Without loss of generality, the amino acid sequences for α_h, ℓ_p, and β_s segments in Figure 1 can be further assigned as follows:

$$\begin{cases} (Ala)_{12}, & \text{for } \alpha_h \text{ segment} \\ (Ala)_4, & \text{for } \ell_p \text{ segment} \end{cases} \quad (1)$$

$$\begin{cases} (Val\text{-}Gly)_3, & \text{for the 1st, 3rd, 5th, 7th } \beta_s \text{ segments} \\ & \text{of the nontilted barrel} \\ (Gly\text{-}Val)_3, & \text{for the 2nd, 4th, 6th, 8th } \beta_s \text{ seg-} \\ & \text{ments of the nontilted barrel} \\ (Val\text{-}Gly)_3, & \text{for all } \beta_s \text{ segments of the right- and} \\ & \text{left-tilted barrels} \end{cases} \quad (2)$$

The choices of amino acid sequences for α_h and ℓ_p and their lengths are the same as in the previous paper.[6] Although the length of the $\ell_p-\alpha_h-\ell_p$ segment is somewhat arbitrary, it must be longer than the distance for a crossover connection between two neighboring β-strands. The choice of amino acid sequence for β_s segments (β-strands) as given by Eq. (2) will ensure that nearest-neighbor residues in adjacent strands are alternately Val and Gly in all of the barrels, i.e., nowhere do two large side chains occur in neighboring positions, in order to avoid large repulsive overlaps.[17] Valine was chosen because it is the most frequently occurring residue in β-strands.[18,19] On the other hand, space limitations inside the barrel are satisfied if there is an alternation of bulky residues (Val) and residues with small or no side chain (preferably Gly) in neighboring positions on adjacent strands. Such a pattern is seen frequently in β-barrels of globular proteins, and hence was adopted in the present study. The whole polypeptide chain was blocked with end groups H– and –OH at its N- and C-termini, respectively.

The procedures to generate various types of α/β barrels are as follows.

Build Up the Core of the Central β-Barrel

By means of the method given by Chou et al.,[16] the left-tilted (Fig. 2), nontilted (Fig. 3), and right-tilted (Fig. 4) idealized parallel β-barrels were built up, respectively. All these barrels contain 8 strands whose amino acid sequences are given in Eq. (2). There are five idealized H-bonds between two adjacent strands for each of these three types of β-barrels, and their H-bond patterns are given in ref. 16. According to the spatial positions of the strands, each of these three types of barrels can be further classified into two subtypes: (1) counterclockwise type (See Figs. 2a–4a) and (2) clockwise type (See Figs. 2b–4b), i.e., if viewed along the direction of the axis Z of a parallel β-barrel,[16] the strands in the former follow a counterclockwise arrangement while the strands in the latter follow a clockwise arrangement (see the legend to Fig. 2 for further explanation). A counterclockwise parallel β-barrel can be used to form a left-handed crossover α/β barrel, and a clockwise parallel β-barrel can be used to form a right-handed crossover α/β barrel.[11]

Connect Two Neighboring β-Strands With an α-Helix

For each of these β-barrels thus generated, all two adjacent strands were connected with a segment $\ell_p-\alpha_h-\ell_p$ (Fig. 1), whose amino acid sequences are given in Eq. (1). After all these connecting operations were done, however, the segment ℓ_p between the last helix and the first strand should be cut off to make the whole $(\alpha/\beta)_8$ barrel structure folded as if from an open chain rather than a closed chain. The process of

connecting two rigidly fixed structures (β_s) with a flexible polypeptide link actually corresponds to a process of geometrical optimization, whose details have been described in the previous papers.[6,20,21] The starting dihedral angles of α_h were those of the computed minimum-energy conformation of an isolated poly(Ala) α-helix,[22] viz. $(\phi, \psi, \omega, \chi^1) = (-68.1°, -38.3°, 180.0°, 60.0°)$. The initial position and orientation of the segment α_h were specified, relative to the β-sheet defined by the two connected strands (β_s), by six external variables, viz. three Euler angles $\bar{\alpha}, \beta, \bar{\gamma}$, and three components t_u, t_v, t_w of a translational vector.[23] The helix segment α_h was initially oriented antiparallel to the two β-strands, and it was placed at the outside of the barrel, 11 Å away from the sheet concerned. Therefore, the initial position and orientation of the segment α_h were defined by Euler angles $(\bar{\alpha}, \beta) = (0°, 180°)$ and translations $(t_u, t_v, t_w) = (0.0, 11.0, 0.0)$ Å and $(0.0, -11.0, 0.0)$ Å for the cases of counterclockwise and clockwise barrels (corresponding to left-handed and right-handed $\beta\alpha\beta$ crossover connections), respectively. Once assigned, all these values were fixed during geometric optimization. Only $\bar{\gamma}$ and the dihedral angles of the two ℓ_p segments, which are attached to the two ends of the segment α_h, were allowed to vary. Therefore, the central part, α_h, of the link segment can be compared with a rigid rod whose only allowable motion is the rotation about its own axis and whose two ends are attached by two flexible "arms" ℓ_ps.

The initial Euler angle $\bar{\gamma}$ that describes rotation of α_h about its own axis and the initial dihedral angles of the two flexible links ℓ_ps attached to the two ends of α_h can be chosen arbitrarily, because they will be determined subsequently by the geometric optimization procedure.[6] In these calculations, the initial dihedral angles assigned for the two flexible "arms" ℓ_ps were $(\phi, \psi, \omega, \chi^1) = (140.0°, 137.2°, 180.0°, 60.0°)$. A random number generator was applied to assign 100 different initial values for the Euler angle $\bar{\gamma}$, yielding 100 different connected conformations for each type of $(\alpha/\beta)_8$ barrel.

Screening Procedure

For each set of 100 $(\alpha/\beta)_8$ barrels generated via the above two steps, a screening procedure was adopted to sift out 10 "candidates" as starting structures for energy minimizations according to the following criteria: (1) the candidate must be a good $(\alpha/\beta)_8$ barrel in the geometric sense, i.e., the objective function[6] F_0 of the geometrical fit for each $\beta\alpha\beta$ connection must be smaller than 0.0025 Å^2, and (2) its conformational energy is one of the 10 lowest among the geometrically good $(\alpha/\beta)_8$ barrels that satisfy criterion (1).

Thus, through the above procedure, there were $6 \times 10 = 60$ starting conformations: 10 for each of the six different types of $(\alpha/\beta)_8$ structures. Among the 10
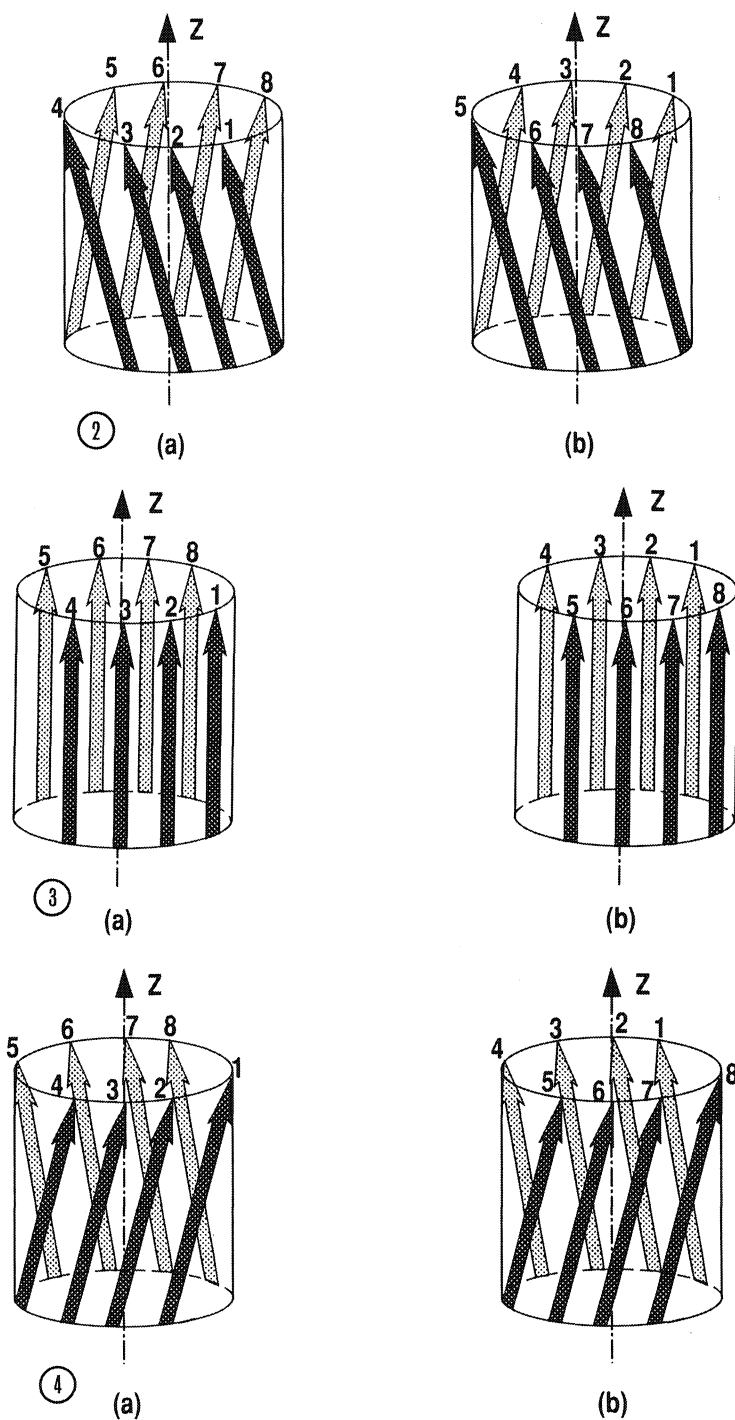
Fig. 2. Schematic illustration of a left-tilted 8-stranded parallel β-barrel. The strands are numbered from 1 to 8 according to the sequential order of the strands. Viewed along the direction of its axis[16] Z, the 8 β-strands follow, in increasing order of number, **(a)** counterclockwise arrangement, and **(b)** clockwise arrangement. The counterclockwise left-tilted parallel β-barrel can be used to form a left-tilted, left-handed crossover α/β barrel. The clockwise left-tilted parallel β-barrel can be used to form a left-tilted, right-handed crossover α/β barrel.

Fig. 3. Schematic illustration of a nontilted 8-stranded parallel β-barrel: **(a)** counterclockwise arrangement, and **(b)** clockwise arrangement. The counterclockwise nontilted parallel β-barrel can

be used to form a nontilted, left-handed crossover α/β barrel. The clockwise nontilted parallel β-barrel can be used to form a nontilted, right-handed crossover α/β barrel. See the legend to Figure 2 for further explanation.

Fig. 4. Schematic illustration of a right-tilted 8-stranded parallel β-barrel: **(a)** counterclockwise arrangement, and **(b)** clockwise arrangement. The counterclockwise right-tilted parallel β-barrel can be used to form a right-tilted, left-handed crossover α/β barrel. The clockwise right-tilted parallel β-barrel can be used to form a right-tilted, right-handed crossover α/β barrel. See the legend to Figure 2 for further explanation.
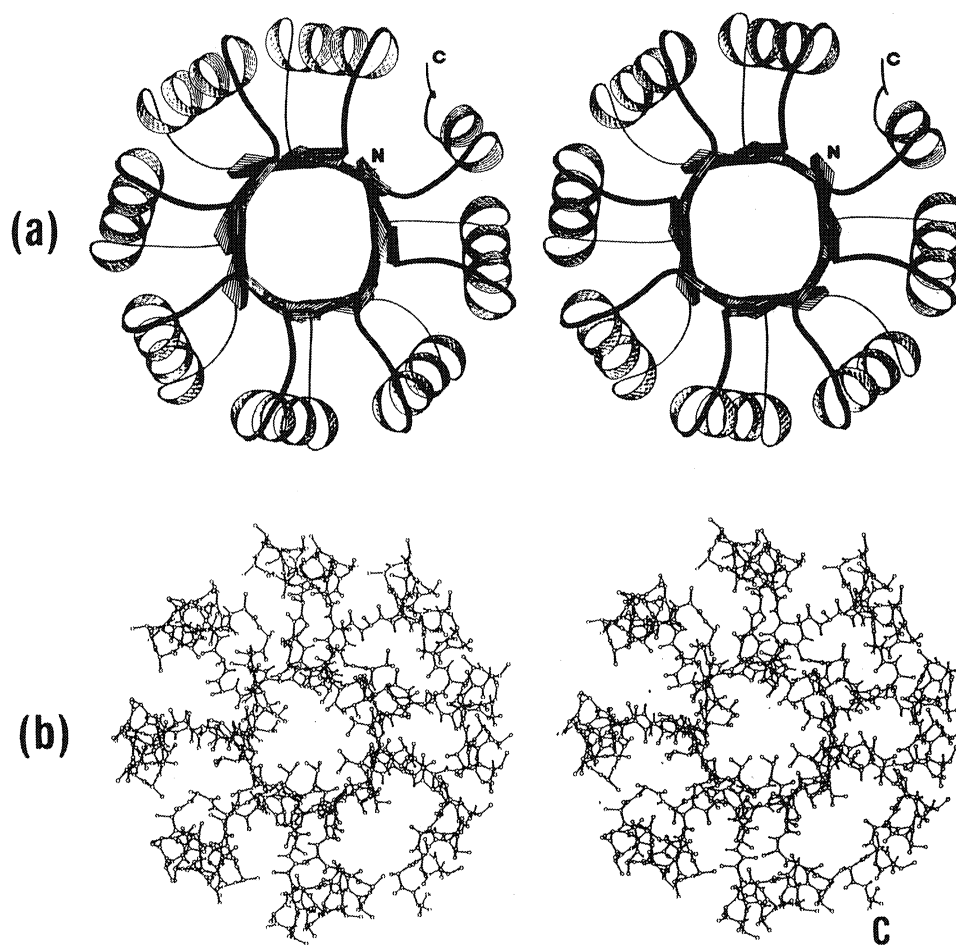
(a)

(b)

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Fig. 5. Stereoscopic drawing of the representative starting conformation, before energy minimization, for the $B_{\parallel}$ type structure, i.e., the left-tilted, left-handed crossover $(\alpha/\beta)_8$ barrel structure: **(a)** the ribbon drawing, and **(b)** the ball and stick drawing, in which only heavy atoms and the amide hydrogens are shown. The

ball and stick drawing is viewed along the axis of the central β-barrel, but the ribbon drawing is viewed opposite to that direction so that the arrows of all the β-strands are pointed to the viewer.

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starting structures in each of these six sets, the one that had the lowest energy was chosen to represent that type of α/β barrel for structural illustration. The stereo drawings of such six representatives are given in Figure 5–10, representing the left-tilted and left-handed crossover (Fig. 5), left-tilted and right-handed crossover (Fig. 6), nontilted and left-handed crossover (Fig. 7), nontilted and right-handed crossover (Fig. 8), right-tilted and left-handed crossover (Fig. 9), and right-tilted and right-handed crossover (Fig. 10) $(\alpha/\beta)_8$ barrels, respectively.

It should be pointed out that there is no guarantee that the lowest energy sequentially connected structure generated by the procedure must be the lowest energy structure after energy minimization. Quite often, however, a sequentially connected structure with a large conformational energy breaks up in the energy minimization step.[20] From this point of view,

therefore, the above screening procedure did effectively help us in finding good starting conformations by promptly excluding many bad ones. Actually, an extensive preliminary calculation has been carried out, indicating that for most cases here the lower the energy of the starting structure, the lower the energy the final structure would reach by energy minimization. Especially, for a given type of α/β structure selecting different starting points might get different energy-minimized values, but it would never change the basic conclusions derived from the 10 starting structures as will be shown later. The goal of the current research is to demonstrate the relative stability among the six types of α/β structures in terms of some rational procedures, but not to search the real unique minimum energy through rigorous mathematical procedures that is technically impossible to date even for a much simpler structure.
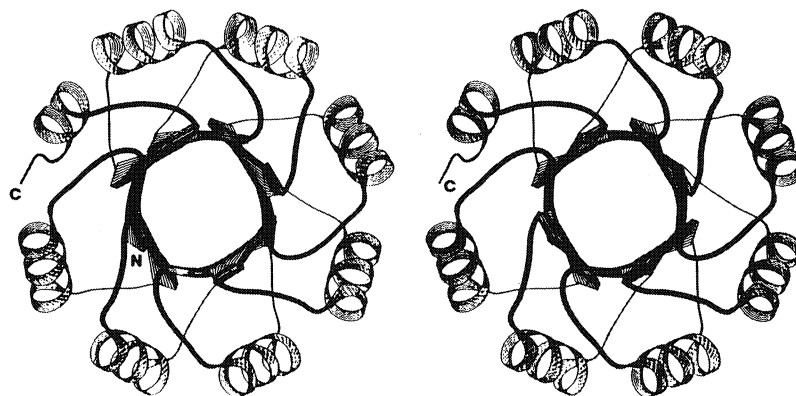
Fig. 6. Stereoscopic ribbon drawing of the representative starting conformation, before energy minimization, for the B_{lr} type structure, i.e., the left-tilted, right-handed crossover $(\alpha/\beta)_8$ barrel structure. Viewed opposite to the direction of the axis of the the central β-barrel so that the arrows of all the β-strands are pointed to the viewer.
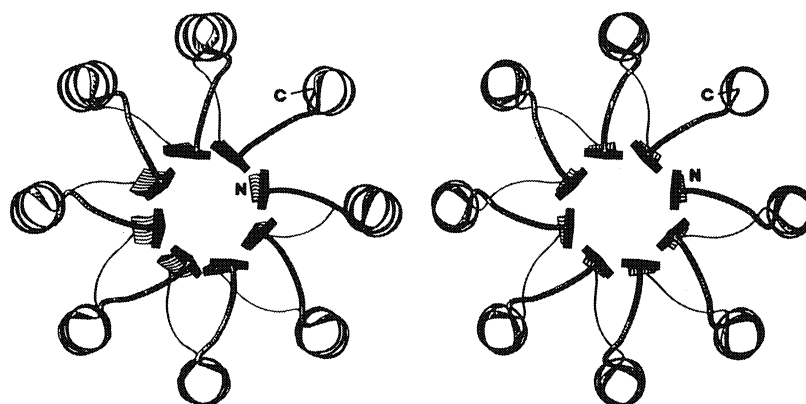

Fig. 7. Stereoscopic ribbon drawing of the representative starting conformation, before energy minimization, for the B_{nl} type structure, i.e., the nontilted, left-handed crossover $(\alpha/\beta)_8$ barrel structure. See the legend to Figure 6 for further explanation.

ENERGY MINIMIZATION

The conformations obtained in the previous section were used as starting points for energy minimization. The energy was computed with the updated version (ECEPP/2) of the ECEPP algorithm (Empirical Conformational Energy Program for Peptides).[24,25] The total energy is the sum of the electrostatic, nonbonded, hydrogen bond, and torsional energies. A general unconstrained optimizing algorithm was used for minimization.[26] The computations were carried out on an IBM 3090/200 computer at Upjohn. The standard conventions for the nomenclature of peptide conformations have been followed.[27]

For each of the 60 starting structures sifted out by the screening procedure as described in the previous section, energy minimization was carried out according to the following steps (the resultant conformation obtained from each step was used as the starting point for the next step).

1. All backbone dihedral angles were kept fixed, and the energy was minimized with respect to all the side chain dihedral angles only, i.e., 228 variables, in order to eliminate side chain atomic overlaps.

2. All the coordinates of the atoms in the β_s segments were *quasifixed*, and the energy was minimized with respect to the backbone dihedral angles of all loop (l_p) and helix (α_h) segments, then followed by step 1. In order to quasifix the coordinates of the atoms in the β_s segments, the following measures were adopted. (a) All the dihedral angles in the β_s segments were fixed. (b) A penalty function was imposed as given below

$$P_f = \Sigma_{m=1}^{8} \{(r_{mi} - r_{mi}^0)^2 + (r_{mj} - r_{mj}^0)^2 + (r_{mk} - r_{mk}^0)^2\} \quad (3)$$

where r_{mi}, r_{mj}, and r_{mk} are the coordinates of the C^α atoms in the i-, j-, and kth residues of the mth strand, respectively, with r^0 standing for the atomic coordinate before the current minimization, and r for that obtained after minimization. For a β-strand
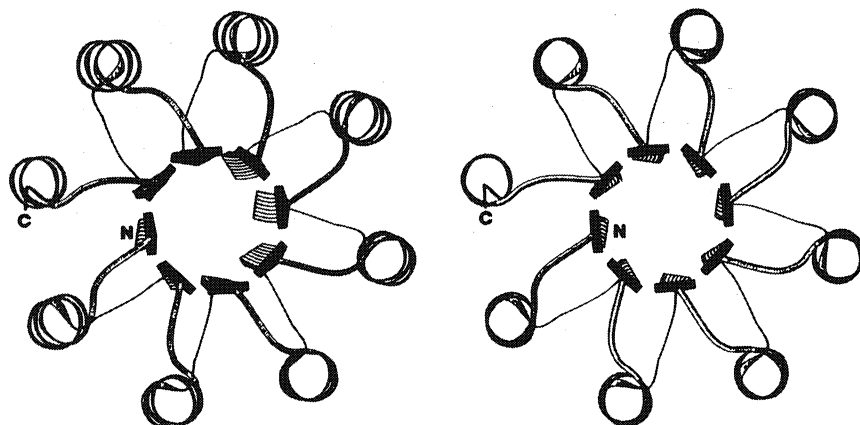
Fig. 8. Stereoscopic ribbon drawing of the representative starting conformation, before energy minimization, for the B_{nr} type structure, i.e., the nontilted, right-handed crossover $(\alpha/\beta)_8$ barrel structure. See the legend to Figure 6 for further explanation.
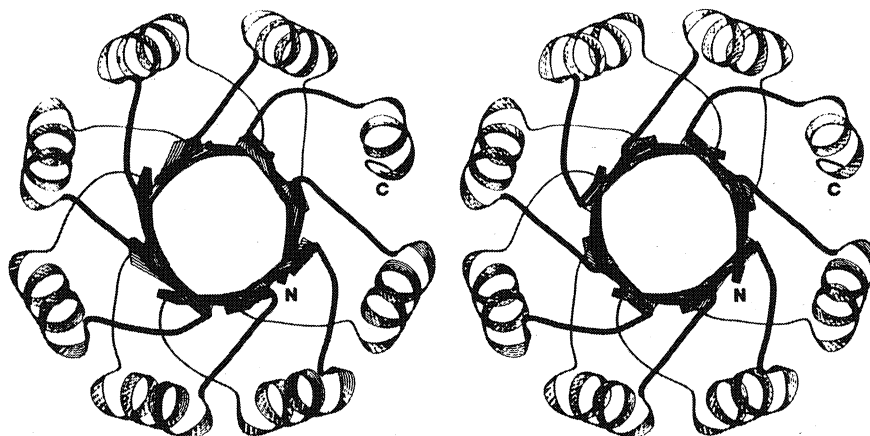

Fig. 9. Stereoscopic ribbon drawing of the representative starting conformation, before energy minimization, for the B_{rl} type structure, i.e., the right-tilted, left-handed crossover $(\alpha/\beta)_8$ barrel structure. See the legend to Figure 6 for further explanation.

with six residues, i, j, and k can be assigned with any three numbers of 1, 2, . . . , 6. In these calculations, (i, j, k) was assigned as (2, 3, 5). Thus, rather than minimizing the total energy E of a chain, the minimization was carried out for the pseudoenergy as given by

$$\Lambda = E + \lambda P_f \qquad (4)$$

where λ is the weight factor, which can be assigned by any value and whose role is to enlarge the effect of the penalty function P_f. Therefore, the greater the weight factor λ is, the stronger the corresponding atoms are held fixed, resulting in the better fixation of the coordinates of the atoms in the β_s segments. The weight factor was assigned as $\lambda = 200$ at this step.

The purpose of combining such a quasi-fixing measure for the coordinates of the atoms in the β_s segments is to reduce the possibility that the hydro-

gen bonds between β-strands might be ruptured during the energy minimization of early stage due to possible atomic overlaps.

3. All the coordinates of the atoms in the β_s segments were quasifixed by assigning the weight factor $\lambda = 50$ in Eq. (4), and then the pseudoenergy Λ was minimized with respect to the backbone dihedral angles of all loop (l_p) segments, then followed by step 1.

4. Release the quasifixed constraint on the β_s segments, i.e., assign $\lambda = 0$. The energy was further minimized only with respect to the backbone dihedral angles of the 8 β-strands (β_s segments), and all the other dihedral angles were fixed. The energy minimization of this step was actually carried out for the inner core of the α/β structure. Again, the energy minimization of this step was completed by repeating step 1.

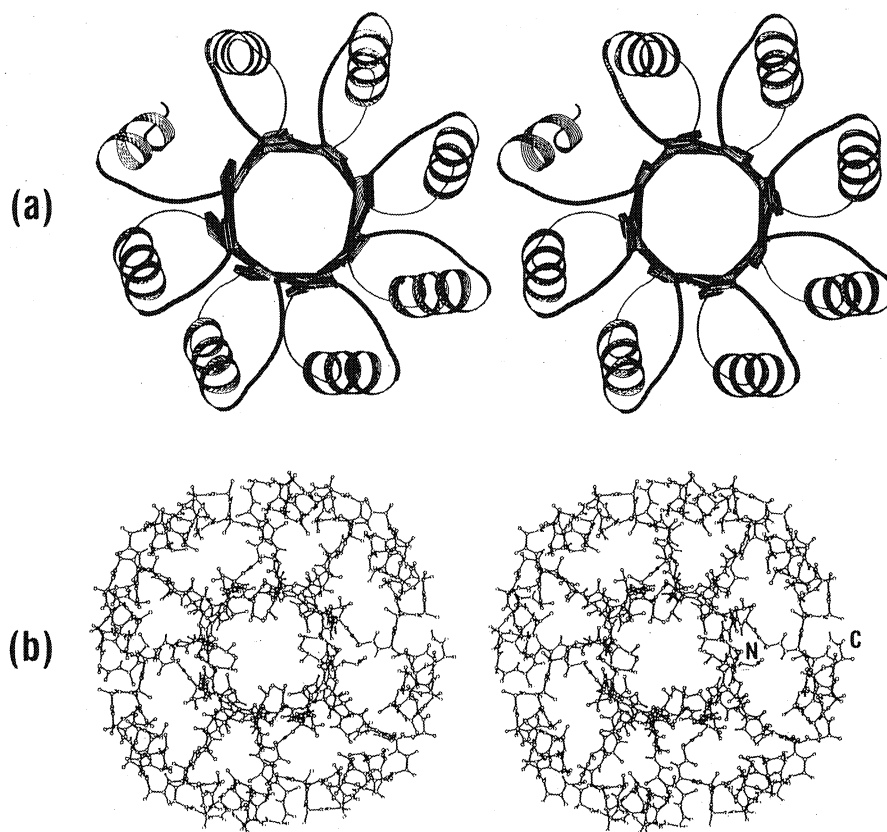5. Finally, the energy was minimized with respect

Fig. 10. Stereoscopic drawing of the representative starting conformation, before energy minimization, for the B_{rr} type structure, i.e., the right-tilted, right-handed crossover $(\alpha/\beta)_8$ barrel structure: **(a)** the ribbon drawing, and **(b)** the ball and stick drawing, in which only heavy atoms and the amide hydrogens are shown. See the legend to Figure 5 for further explanation.

to all dihedral angles of the entire chain, i.e., 840 variables.

In the process of energy minimization, the central barrel of the $(\alpha/\beta)_8$ structure was monitored to see whether it was broken or not. Such a monitor was promptly realized by showing the distances between the atoms involved in forming the hydrogen bond $C' = O \cdots H - N$ holding two neighboring strands, i.e., the distance r_{OH} between atoms O and H, and the distance $r_{C'N}$ between atoms C' and N. These distances in an idealized 8-stranded parallel β-barrel are[16]

$$r_{OH} = 2.0 \text{ Å}$$
$$r_{C'N} = \sqrt{(2.0 \sin 20°)^2 + [2.0 \cos 20° + 2.23 \cos(\frac{180°}{8})]^2} \text{ Å} \quad (5)$$

Although there is no strict cutoff about the range of hydrogen bonding, it is generally believed that the stretching limitation for a hydrogen bond is within 0.5 Å. Therefore, a H-bond is considered to be intact or exist when (1) 1.5 Å $< r_{OH} <$ 2.5 Å, and (2) 3.5 Å $< r_{C'N} <$ 4.5 Å; otherwise it is highly deformed or broken. A β-barrel is considered to be broken if all H-bonds between any two of its neighboring strands are broken.

RESULTS AND DISCUSSION

For each set of the 10 structures belonging to a same type of α/β structure, the one whose energy was the lowest after energy minimization was chosen as a representative of that type structure for the following discussion. The data listed in Tables I–IV were also derived from these representative structures.

After energy minimizations, the central parallel β-barrel remained unbroken only in the B_{ll} or B_{rr} structure, i.e., the left-tilted, left-handed crossover $(\alpha/\beta)_8$ structure or the right-tilted, right-handed crossover $(\alpha/\beta)_8$ structure, but it was broken in all the other types of $(\alpha/\beta)_8$ structures, as shown in Table I. This indicates that it is energetically unfavorable for a parallel β-barrel to dwell as an inner core in the B_{lr}, B_{nl}, B_{nr}, and B_{rl} type structures. The stereo drawings for the energy-minimized B_{ll} and B_{rr} structures, which each contains an unbroken central β-barrel, are given in Figures 11 and 12, respec-

TABLE I. The Outcome of Minimizing the Energies of Six Types of $(\alpha/\beta)_8$ Structures*

Type of starting $(\alpha/\beta)_8$ structure[†]	Energy (kcal/mol)				General appearance of of the central β-barrel
	E_{es}[‡]	E_{nb}[§]	E_{tor}[**]	E_{tot}[††]	
B_{ll}	1110.1	−1242.0	45.2	−86.7	Parallel β-barrel with 8 left-tilted and left-handed twisted strands
B_{lr}	—	—	—	—	Broken
B_{nl}	—	—	—	—	Broken
B_{nr}	—	—	—	—	Broken
B_{rl}	—	—	—	—	Broken
B_{rr}	1096.0	−1339.0	30.9	−212.1	Parallel β-barrel with 8 right-tilted and right-handed twisted strands

*Only the representative structure of each type is listed. The representative structure is the one which has the lowest minimized energy among the structures of that type, as defined in the text.
[†]B_{ll} represents the left-tilted, left-handed crossover $(\alpha/\beta)_8$ barrel, B_{lr} the left-tilted, right-handed crossover $(\alpha/\beta)_8$ barrel, B_{nl} the nontilted, left-handed crossover $(\alpha/\beta)_8$ barrel, B_{nr} the nontilted, right-handed crossover $(\alpha/\beta)_8$ barrel, B_{rl} the right-tilted, left-handed crossover $(\alpha/\beta)_8$ barrel, and B_{rr} the right-tilted, right-handed crossover $(\alpha/\beta)_8$ barrel.
[‡]Electrostatic component of the total conformational energy.
[§]Nonbonded component of the total conformational energy.
[**]Torsional component of the total conformation energy.
[††]Total conformational energy of the entire $(\alpha/\beta)_8$ molecule; i.e., $E_{tot} = E_{es} + E_{nb} + E_{tor}$.
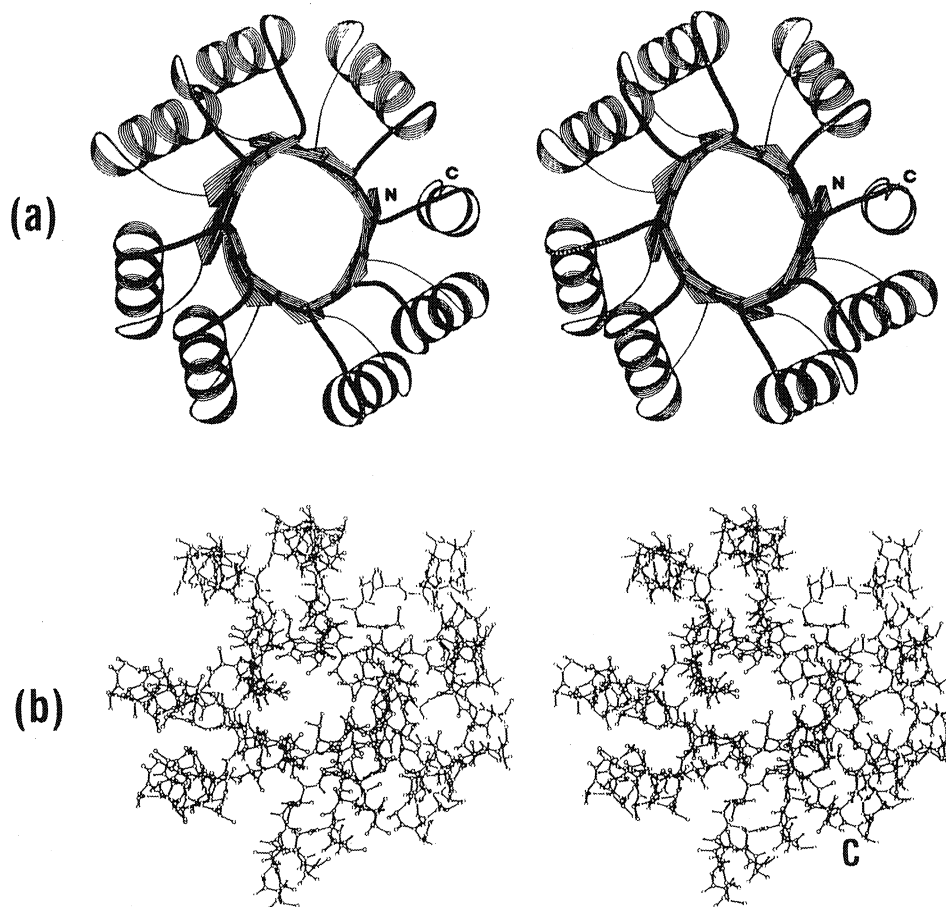

Fig. 11. Stereoscopic drawing of the energy-minimized B_{ll} structure, i.e., the left-tilted, left-handed crossover $(\alpha/\beta)_8$ barrel: (a) the ribbon drawing, and (b) the ball and stick drawing, in which only heavy atoms and the amide hydrogens are shown. See the legend to Figure 5 for further explanation.

tively. It is also shown in Table I that the energy-minimized B_{rr} structure is 125.4 kcal/mol lower in energy than the energy-minimized B_{ll} structure,

elucidating from an energetic point of view why the observed α/β barrels in proteins are always of right tilt and right-handed crossover connection. Energy
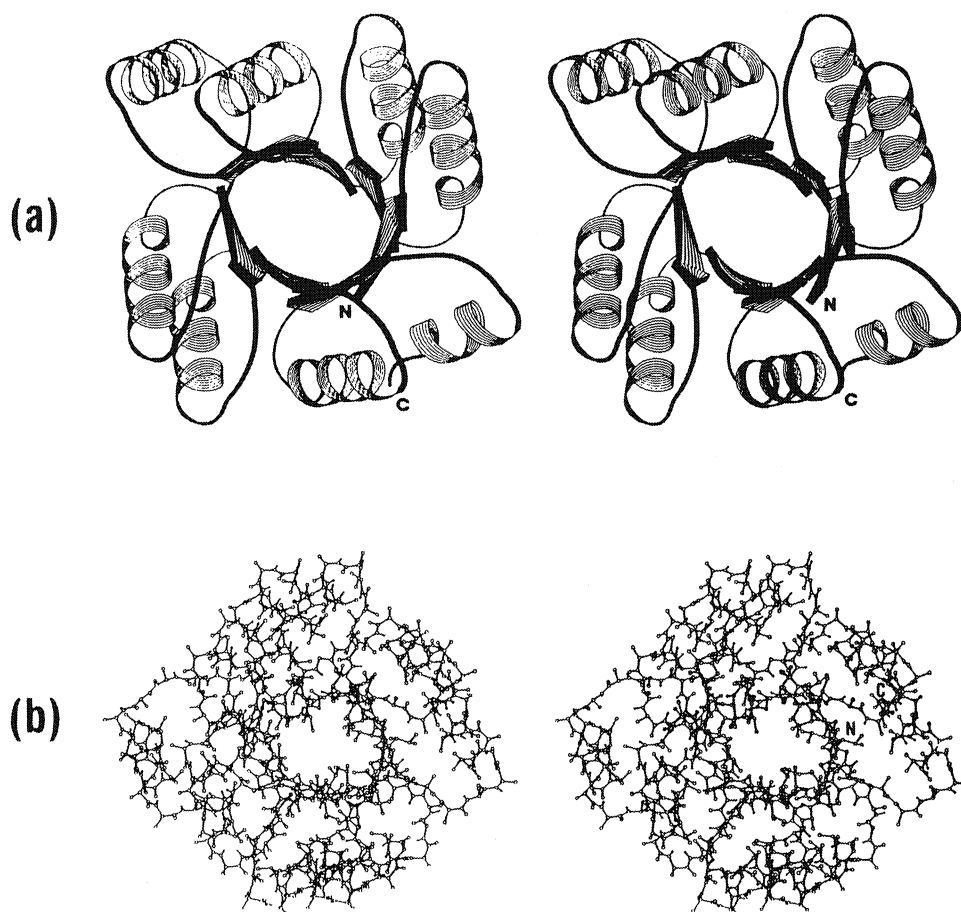
Fig. 12. Stereoscopic drawing of the energy-minimized B_{rr} structure, i.e., the right-handed, right-crossover $(\alpha/\beta)_8$ barrel: (a) the ribbon drawing, and (b) the ball and stick drawing, in which only heavy atoms and the amide hydrogens are shown. See the legend to Figure 5 for further explanation.

in favor of the B_{rr} structure is largely contributed from the nonbonded interactions. It is interesting to see from Table I that the electrostatic energies in both B_{rr} and B_{ll} structures are positive. This can be understood because the 8 peripheral α-helices around the central parallel β-barrel are oriented in a manner closer to a parallel than an antiparallel arrangement (Figs. 11–12). However, a parallel arrangement of neighboring α-helices is unfavorable in electrostatic interactions between the helices caused by the large dipole moments of the α-helices.[28–30] Therefore, the positive electrostatic interaction energy is a common feature for the α/β barrel structures. More discussion about energies contributed from different segments of the α/β structures will be given later.

Before energy minimization the six types of $(\alpha/\beta)_8$ structures each contains an idealized parallel β-barrel (Figs. 2–4), in which there are 5 H-bonds between its two neighboring β-strands, for a total of 5 × 8 = 40 H-bonds.[16] After energy minimizations for the B_{lr}, B_{nl}, B_{nr}, and B_{rl} type structures, however, their central β-barrels were all broken as reflected

by the fact that the H-bonds in at least one pair of neighboring β-strands were totally ruptured for all these barrels. Only for the B_{ll} and B_{rr} structures did the energy minimization not break the H-bonds in their inner cores of barrels. For these two energy-minimized structures each of which represents its own type of the lowest energy thus found, the average length of H-bonds in each pair of β-neighboring strands is listed in Table II. It is seen from these values that none of them deviates more than 0.12 Å from the corresponding values of an idealized H-bond for an 8-stranded parallel β-barrel, indicating that the H-bonds of the central β-barrels in the energy-minimized B_{ll} and B_{rr} structures are quite normal. This can also been seen by the corresponding stereo drawings as given in Figures 11 and 12.

Why were the β-barrels in B_{lr}, B_{nl}, B_{nr}, and B_{rl} type structures broken after energy minimization? Let us consider the case of the B_{nl} and B_{nr} type structures first. The β-barrel contained in B_{nl} or B_{nr} type structure is a non-tilted one (Fig. 3). It has been demonstrated[16] that given the same length of H-bonds between β-strands, a nontilted β-barrel has a

TABLE III. Geometric Parameters Characterizing the Central β-Barrels in the Energy-Minimized B_{ll} and B_{rr} Structures

	B_{ll}			B_{rr}		
	$<\delta>$* (deg)	$\theta^{\dagger}$ (deg)	$d_r^{c\ddagger}$ (Å)	$<\delta>$* (deg)	$\theta^{\dagger}$ (deg)	$d_r^{c\ddagger}$ (Å)
Strand						
1	−14.8	31.5	7.3	49.9	−36.7	7.9
2	−23.4	30.9	7.5	51.0	−31.1	6.3
3	−18.1	29.1	6.9	36.0	−22.5	6.4
4	−25.5	30.0	7.0	42.0	−32.6	8.3
5	−16.3	30.9	7.2	41.4	−38.3	7.7
6	−25.1	33.1	7.5	45.0	−32.2	6.4
7	−17.4	29.4	6.9	36.8	−25.2	6.5
8	−21.9	29.4	7.1	45.6	−34.0	8.1
Average of 8 strands	−20.3	30.4	7.2	43.5	−31.6	7.2
$<\Omega_0>^{\S}$ (deg)	22			−30		
$\Omega_{\alpha\beta}^{\dagger\dagger}$ (deg)	180 ± 20°			180 ± 18°		

*The average twist of β-strand. See Chou et al.[38] for the definition of δ. The right-handed twist, left-handed twist, and nontwist correspond to δ > 0, δ < 0, and δ = 0, respectively.

†The tilted angle of a constituent β-strand to the central axis of a barrel.[16] The right-tilted, left-tilted, and nontilted β-strands correspond to θ < 0, θ > 0, and θ = 0, respectively.

‡The radial distance from the central axis of a β-barrel to each of its strands. The data of d_r can be used to describe the shape of cross section of a β-barrel, as shown in Figure 13.

§The average orientational angle[22] between two neighboring α-helices.

††The packing angle[23] of an α-helix against the β-sheet formed by the two strands connected by the helix via a crossover.
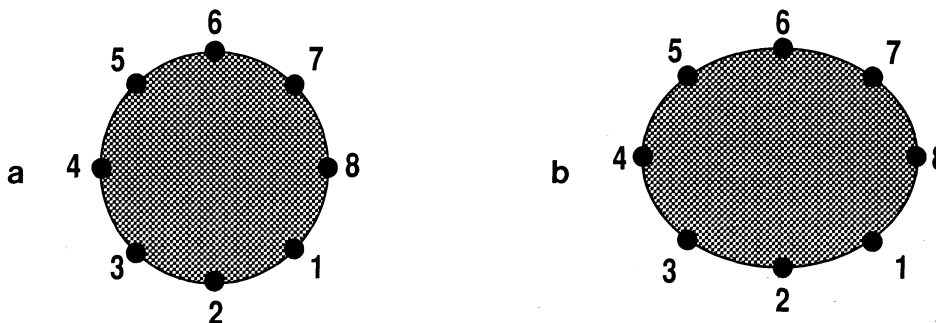

Fig. 13. The cross section of (a) the idealized 8-stranded parallel β-barrel in which the radial distances from the axis of the barrel to all the constituent strands are the same, i.e, d_r = 7.3 Å,[16] and (b) the central β-barrel of the energy-minimized B_{rr} structure in which the values of d_r are different for the 8 constituent strands as shown in Table III. The shape of the cross section in (a) is a circle, but that in (b) is an ellipse.

an encouraging sign because the elliptical cross section is a common geometric feature for observed β-barrels in proteins.[3,5,33,34] Therefore, after energy minimization the β-barrel in the B_{rr} structure is more close to the observed β-barrels. As a further demonstration, a skeleton stereo drawing to show the fitness of backbone atoms between the central β-barrel of the energy-minimized B_{rr} structure and the parallel 8-stranded β-barrel in TIM is given in Figure 14, where the computed β-barrel was drawn in red and the observed β-barrel was drawn in blue. The atomic coordinates for TIM were obtained from the Brookhaven Protein Data Bank, based on the work by Banner et al.[1] In comparison with the previous stereo drawing showing the fitness between the corresponding idealized β-barrel and the β-

barrel in TIM (see Fig. 9a of ref. 16), it can be seen that the current fitting was improved. The better fitting is also indicated by the smaller value of the root-mean-square (RMS) fit, which is 1.4 Å now vs. 1.6 Å of the previous value.[16] It should be pointed out that such a change in shape of the cross section from a circle to to an ellipse did not occur when minimizing the energy of an idealized β-barrel consisting of sequentially separate β-strands (see Fig. 2 of ref.17). Therefore, the elliptical cross section as generally occurs in observed β-barrels was caused by the effect of the connecting segments between the β-strands.

The arrangements of the 8 α-helices at the periphery of the energy-minimized B_{ll} and B_{rr} structures are as follows. The average orientational angle[22,35]
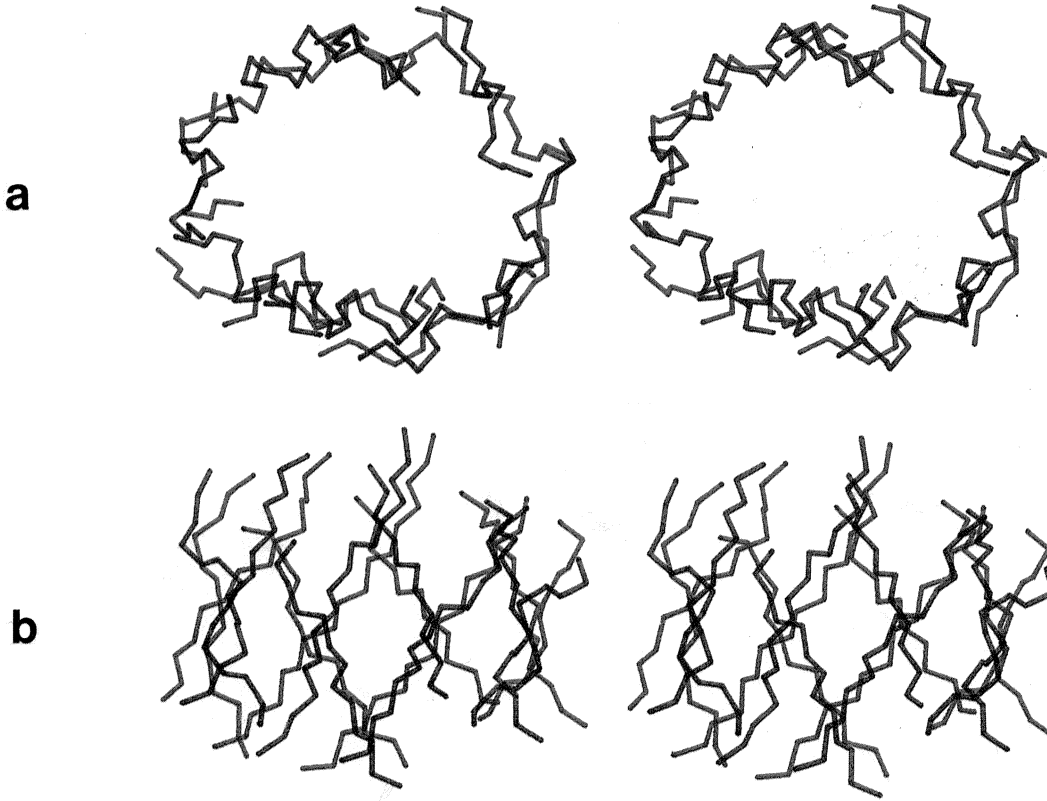
Fig. 14. Stereoscopic skeleton drawing to show the fitness between the central parallel β-barrel of the energy-minimized B_{rr} structure and the observed parallel β-barrel in TIM (RMS) deviation = 1.4 Å): **(a)** viewed along the axis of β-barrel, and **(b)** viewed from the side of β-barrel. Only the β-barrel backbone atoms N, C^α, and C' were used for the least-squares fitting.[16,33] The observed β-barrel was drawn in blue and the computed β-barrel drawn in red.

$< \Omega_0 >$ between two neighboring helices is 22° for the B_{ll} structure and −30° for the B_{rr} structure; i.e., the 8 α-helices in the former follow a left-handed spiral around the barrel axis and those in the latter follow a right-handed spiral around the barrel axis. The packing angle[23] $\Omega_{\alpha\beta}$ of an α-helix against the β-sheet formed by the two β-strands it connects is 180° ± 20° for the B_{ll} structure and 180° ± 18° for the B_{rr} structure, i.e., the axes of the α-helices are approximately parallel to the β-strands. Both of these features regarding the arrangement of α-helices as occurred in the low-energy B_{rr} structure are usual in the observed α/β barrels.[2,3,5,11]

In order to compare and analyze the energetics contributed from different segments of the $(\alpha/\beta)_8$ barrel structure and their interactions, let us separate the total conformational energy E_{tot} of the entire $(\alpha/\beta)_8$ molecule into the terms as defined below:

E^α_{intra} = Sum of the energies of the 8 individual constituent α-helices (α_hs)

E^α_{inter} = Total intersegment energy among the 8 α-helices

$E^\alpha_{tot} = E^\alpha_{intra} + E^\alpha_{inter}$

E^β_{intra} = Sum of the energies of the 8 individual constituent β-strands (β_ss)

E^β_{inter} = Total intersegment energy among the 8 β-strands

$E^\beta_{tot} = E^\beta_{intra} + E^\beta_{inter}$

$E^{\alpha/\beta}_{inter}$ = Total interset energy between α-helices and β-strands, i.e., the interaction energy between the outer helices and inner core of barrel   (6)

$E^{\alpha/\beta}_{tot} = E^\alpha_{tot} + E^\beta_{tot} + E^{\alpha/\beta}_{inter}$.

E^{loop}_{intra} = Sum of the energies of the 15 individual loops (ℓ_ps)

E^{loop}_{inter} = Total intersegment energy among the 15 loops

$E^{loop}_{tot} = E^{loop}_{intra} + E^{loop}_{inter}$

$\bar{E}^{loop}_{tot} = E^{loop}_{tot} + \epsilon$, where ϵ is the interaction energy between the loops and all the other part of the molecule

$\bar{E}^{loop}_{tot}$ in the above equation is called *associated loop*

TABLE IV. Various Energetic Terms Characterizing the Energy-Minimized B_{11} and B_{rr} Structures*

Type of $(α/β)8$ barrel	Energy of $α_h$ set (kcal/mol)			Energy of $β_s$ set (kcal/mol)			Energy of $α_h/β_s$ set (kcal/mol)		Loop-related energy (kcal/mol)					Energy of entire molecule
	$E^α_{intra}$	$E^α_{inter}$	$E^α_{tot}$	$E^β_{intra}$	$E^β_{inter}$	$E^β_{tot}$	$E^{α/β}_{inter}$	$E^{α/β}_{tot}$	E^{loop}_{intra}	E^{loop}_{inter}	E^{loop}_{tot}	$ε$	$\bar{E}^{loop}_{tot}$	E_{tot}
B_{11}	-45.1	-24.2	-69.3	224.8	-215.5	9.3	-59.9	-119.9	393.4	-45.0	348.4	-315.2	33.2	-86.7
B_{rr}	-45.9	-36.1	-82.0	196.3	-201.2	-4.9	-50.2	-137.1	286.5	-14.4	272.1	-347.1	-75.0	-212.1

*See Eq. (6) for the definition of each of the energetic terms.

energy, which is defined by augmenting E^{loop}_{tot} to incorporate $ε$, the interaction term between the loop segments and the other part of the $(α/β)_8$ molecule,[20,21] and hence represents the total energy associated with the loops. From Eq. (6) we obviously have

$$E_{tot} = \bar{E}^{loop}_{tot} + E^{α/β}_{tot} \qquad (7)$$

Listed in Table IV are the values of the energetic terms as defined in Eq. (6) for the energy-minimized B_{11} and B_{rr} structures, respectively. As we can see, the total conformational energy in the B_{rr} structure is 125.4 kcal/mol lower than that in the B_{11} structure. From Eq. (7) and Table IV we can further see that of such an energy gap 108.2 kcal/mol is from $\bar{E}^{loop}_{tot}$ and only 17.2 kcal/mol is from $E^{α/β}_{tot}$. Therefore, it is the associated loop energy $\bar{E}^{loop}_{tot}$ which plays the major role in favor of the right-tilted and right-handed crossover $(α/β)_8$ structure. This is because the intraloop energy E^{loop}_{intra} and the interaction $ε$ between the loop segments and the other part of the molecule are much more favorable to B_{rr} than B_{11}. Moreover, the interhelix energy $E^α_{inter}$ and intrastrand energy $E^β_{intra}$ are favorable in making $E^{α/β}_{tot}$ have lower energy in B_{rr} than in B_{11}. This is completely consistent with the computed results on the packing of α-helices and the twist of β-strands. Recall that the average orientational angle $< Ω_0 >$ between two neighboring helices in the B_{11} structure is 22° and that in the B_{rr} structure is -30° (Table III). It was indicated in the previous paper[35] that the packing between two α-helices has a lower energy at the arrangement with the orientational angle $Ω_0$ around -30° than 22°. That is why the interhelix energy $E^α_{intra}$ is lower in the B_{rr} structure than in the B_{11} structure. On the other hand, a β-strand generally has lower energy when it is right-handed twisted than left-handed twisted.[36-38] In harmonizing with the right-tilted and right-handed crossover geometry, all the β-strands in the B_{rr} structure are in the lower energy form of right-handed twisting, but in the B_{11} structure the presence of a left-tilted barrel and left-handed crossover connection forces the β-strands into the energetically less favorable left-twisted form (Table III). That is why the intrastrand energy $E^β_{intra}$ is lower in the B_{rr} structure than in the B_{11} structure.

Therefore, the calculated energy in favor of the

right-tilted, right-handed crossover α/β barrel is correlated with the fact that right-handed twisted β-sheets are more stable than left-handed twisted or non-twisted β-sheets.[36-38] Similar correlation[6,20] has also been found in βαβ and Rossmann fold structures. The highly consistent results derived from different types of structures indicate that although the energetic calculations in this paper were performed on a particular sequence of polypeptide, the applicability of the derived conclusions to proteins is general.

CONCLUSIONS

Six different types of α/β barrels, classified according to the tiltedness of the β-strands and the handedness of crossover connection between two neighboring β-strands, were generated and energy-minimized. After energy minimizations, only in the right-tilted and right-handed crossover connection α/β structure or in the left-tilted and left-handed crossover connection α/β structure did the central β-barrel remain unbroken. The central β-barrels in all the other four types of α/β structures were destroyed after energy minimizations, as reflected by the fact that the original arrangement of hydrogen bonds of cylindrical pattern in these structures was substantially damaged so that the β-strands were no longer held to have a general shape of a barrel. The β-barrel contained in the nontilted and either right-handed or left-handed crossover α/β structure is unstable because its radius is smaller than those in the corresponding tilted α/β structures, suggesting that a conformational change from a nontilted β-barrel to a tilted one would ease the repulsion among the crowded internal side chains.[16] However, driven by energy minimization rather than nature, such a conformational change must end with an irreversible breakage of the barrel. The β-barrels in the left-tilted and right-handed crossover α/β structure and in the right-tilted and left-handed crossover α/β structure are also unstable because the distances for the crossover connections between neighboring β-strands of the central barrels in these two structures are longer than those of the others, representing more strained[31] and less energetically favorable.[6] However, between the two α/β structures whose central β-barrels remained unbroken after energy minimizations, the right-tilted and right-handed cross-

over α/β structure (B_{rr}) is 125 kcal/mol lower in energy than the left-tilted and left-handed crossover α/β structure (B_{ll}). Such a large energy gap is mainly caused by the associated loop energy which plays a key role in favor of the right-tilted and right-handed crossover $(\alpha/\beta)_8$ structure, as reflected by the fact that both the intraloop energy and the interaction between the loop segments and the other part of the molecule are much more favorable in this structure (B_{rr}) than its left-handed counterpart (B_{ll}), as shown in Table IV. Moreover, the interhelix energy and intrastrand energy provide additional contributions in favor of the right-tilted and right-handed crossover α/β structure (B_{rr}).

The results presented here indicate that the right-tilted and right-handed crossover α/β barrel structure is the energetically most stable type of structure among the six types of α/β structures. This is fully in agreement with the observations that so far all the known α/β barrels in proteins are right-tilted and right-handed crossover connected. Besides, all the β-strands in the energetically most stable $(\alpha/\beta)_8$ barrel thus found are strong right-handed twisted, which is a common feature of observed β-barrels in proteins.[2,5,7,9,10,32,33] The value of root-mean-square fits between the computed parallel β-barrel and the observed 8-stranded parallel β-barrel in TIM further indicates that there is a better fitting after energy minimization than before energy minimization. All these results support the principle that it is possible to account for the main features of frequently occurring folding arrangements in proteins in terms of conformational energy calculations even for very complicated structures such as $(\alpha/\beta)_8$ barrels.

ACKNOWLEDGMENTS

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